

Set → a collection of things where you can tell exactly what is and isn't part of the collection.

- We usually use capital letters to stand for sets.

Element (or member) → one of the things that is part of a set.

Ways of writing sets

- Always put braces { } around sets.

Roster Notation → Just list the elements in the set (useful for small sets)

- Can use ... to show members being left out.
 - { Algona, Emmetsburg, Estherville, Spencer, Spirit Lake }
 - { 4, 7, 13 }
 - { Mon., Tues. ... Fri. }
 - { 2, 4, 6, 8, 10 ... }

Set-Builder Notation → Give a rule that tells what elements are in the set

- { x | x is an instructor at ILCC }
- The vertical line is read "where" or "such that".
- We read this as "the set of all x where x is an instructor at ILCC".
- Another example:

$$\{ x \mid x < 10, x \geq 0, \text{ and } x \text{ is even} \}$$

Element notation

- \in means "is an element of"
- $P \in A$ means p is one of the members in set A .

Equal Sets → Have exactly the same elements.

$$\{ x \mid x < 10, x \geq 0, \text{ and } x \text{ is even} \} = \{ 0, 2, 4, 6, 8 \}$$

Equivalent Sets → have the same number of elements.

- { a, b, c } and { p, q, r } are equivalent.

Cardinality means the number of elements in a set

- Notation $n(A)$
- For example $n(\{p, q, r, s\}) = 4$

You should **not** repeat elements in a set. If elements are repeated in an example, ignore the repeats.

- { 1, 2, 2, 3, 4, 4, 4, 5 } is not right.
- Instead put { 1, 2, 3, 4, 5 }

Empty Set → A set with no members

- { } and \emptyset are symbols for the empty set
- { x | x is an odd number divisible by 2 } = { }

The symbol **N** means the set of **natural numbers**, which is { 1, 2, 3, 4, 5, ... }

Universal set → a set that contains **EVERY** possible element that could be part of a given situation.

- Everything you are allowed to use for a problem.

Complement → "Everything but"

- all the elements in the universal set **except** what is in a given set.
- NOTATION: A'

EXAMPLE: Suppose the universal set is

{ x | x is a day of the week }. If $A = \{ \text{Mon., Tues., Wed.} \}$, what is A' ?

$$A' = \{ \text{Thur.}, \text{Fri.}, \text{Sat.}, \text{Sun.} \}$$

EXAMPLE:

$$U = \{ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 \}$$

$$A = \{ 2, 4, 6, 8, 10 \}$$

What is A' ?

$$A' = \{ 1, 3, 5, 7, 9 \}$$

Subset

- Notation: \subseteq
- $A \subseteq B$ means every element of A is also an element of B .
- Everything in A is **contained in** B .

So ...

$$\{ \text{Iowa}, \text{Wisconsin} \} \subseteq \{ x \mid x \text{ is a state of the USA} \}$$

- Every set is a subset of itself.
 $\{ 1, 2, 3, 4 \} \subseteq \{ 1, 2, 3, 4 \}$
- The empty set is a subset of everything.
 $\emptyset \subseteq \{ 1, 2, 3, 4 \}$

Proper Subset \rightarrow A subset that isn't the set itself.

- Notation: \subset
 $\{ 1, 2 \} \subset \{ 1, 2, 3, 4, 5 \}$
- Proper subsets have to be **smaller** than the original set.

Notation \rightarrow $\not\subseteq$ means "not a subset"

- Could have totally different elements

$$\{ a, b \} \not\subseteq \{ 1, 2, 3 \}$$

- 1st set could be bigger than 2nd.

$$\{ a, b, c \} \not\subseteq \{ a, b \}$$

How many subsets does a set have?

- If $n(A) = 2$, then A has 2^2 or 4 subsets.
- If $n(A) = 3$, then A has 2^3 or 8 subsets.
- If $n(A) = 4$, then A has 2^4 or 16 subsets.

In general, every set has 2^n subsets, where "n" is the number of elements in the set.

There will always be $2^n - 1$ **proper** subsets.

UNION

- Symbol \cup
- Combining **EVERYTHING** in 2 or more sets

$$A \cup B = \{ x \mid x \in A, x \in B, \text{ or } x \text{ is in both } A \text{ and } B \}$$

- Example:

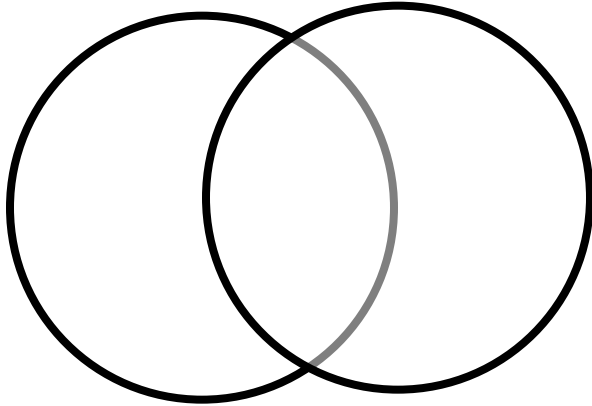
$$P = \{ 1, 2, 3, 4, 5 \}$$

$$Q = \{ 5, 6, 7 \}$$

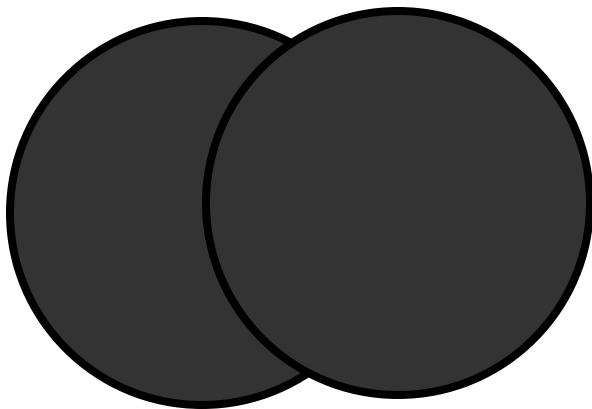
$$P \cup Q = \{ 1, 2, 3, 4, 5, 6, 7 \}$$

1st Set

2nd Set



Union



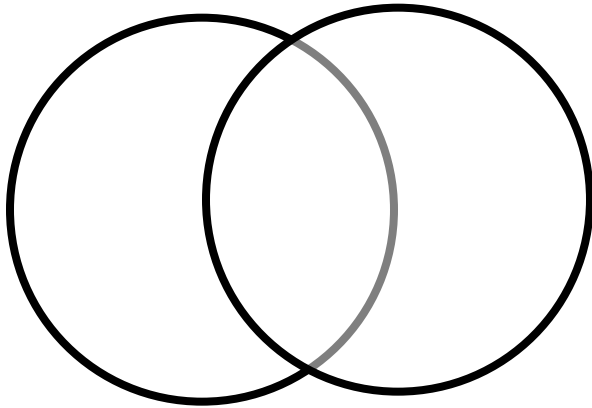
Intersection

- Symbol \cap
- The things that are in 2 or more sets *AT THE SAME TIME*.
- What **overlaps** between different sets

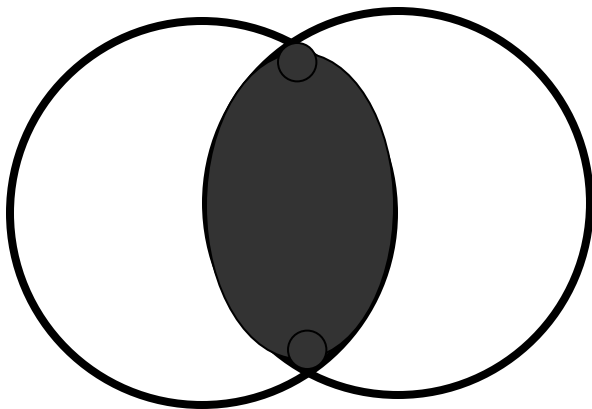
$$A \cap B = \{x \mid x \in A \text{ and } x \in B\}$$

1st Set

2nd Set



Intersection



- Example:

$$P = \{ 1, 2, 3, 4, 5 \}$$

$$Q = \{ 5, 6, 7 \}$$

$$P \cap Q = \{ 5 \}$$

- Example:

$$E = \{ 1, 2, 3, 4, 5 \}$$

$$F = \{ 6, 7, 8, 9, 10 \}$$

$$E \cap F = \emptyset$$

(E and F are called **disjoint** sets.)